

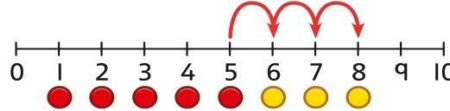
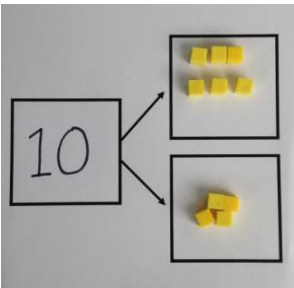
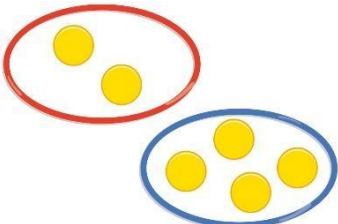
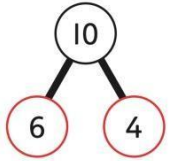


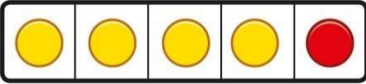
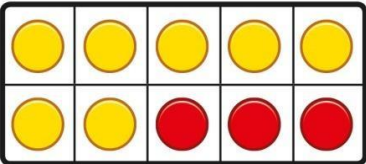
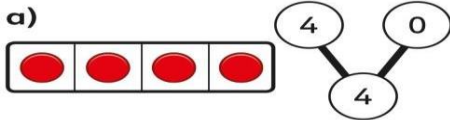
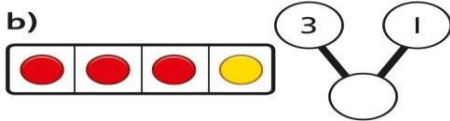
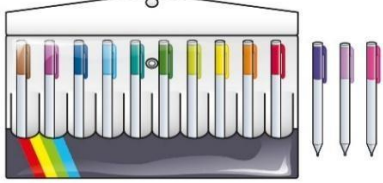
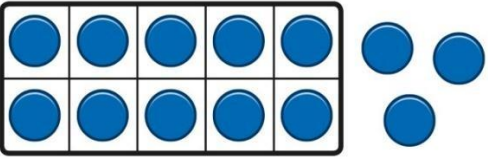
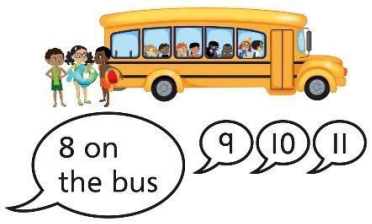
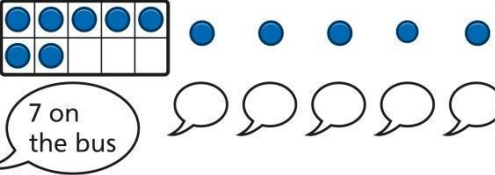
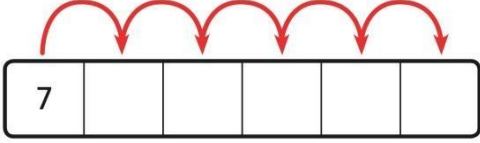

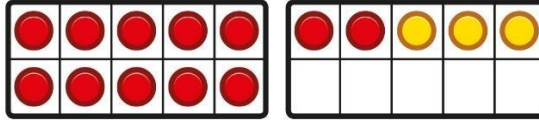

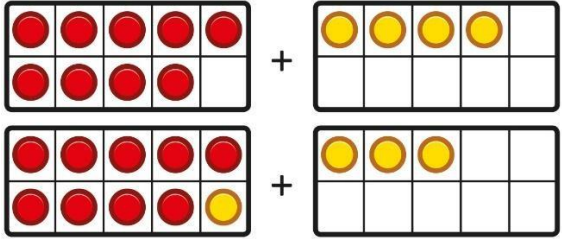
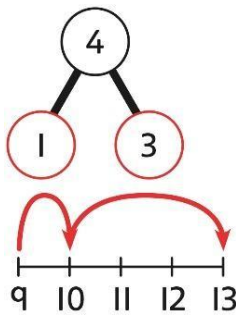

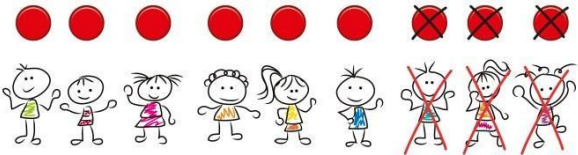
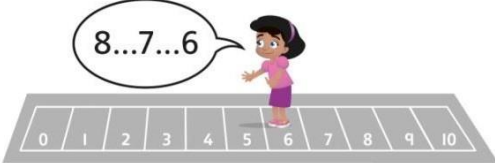
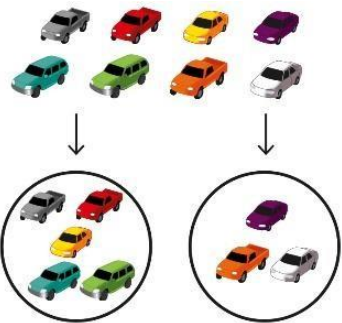
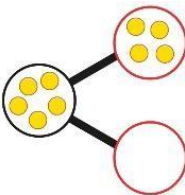
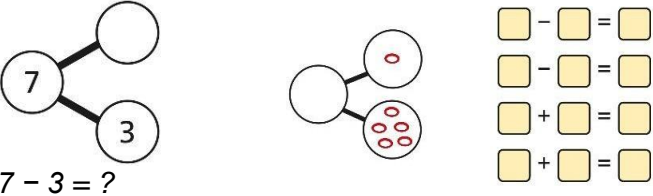

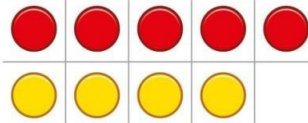
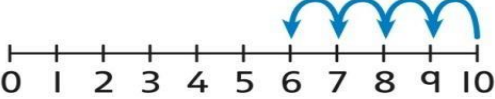



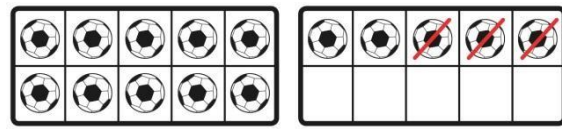

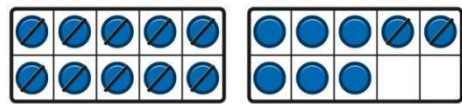
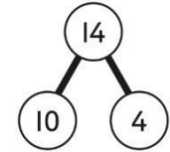
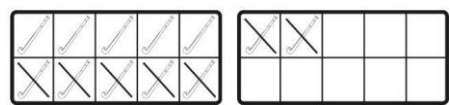
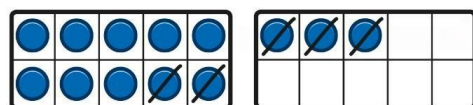
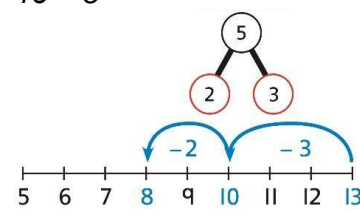
Year 1

| Year 1                   | Concrete   | Pictorial  | Abstract  |
|--------------------------|--|--|---|
| Counting and adding more | <p>Children add one more to a group to find one more.</p>  $8 + 1 = 9$  | <p>Children add one more cube or counter to a group to represent one more.</p>  <p><i>One more than 4 is 5.</i></p>                                | <p>Use a number line to understand how to link counting on with finding one more.</p>  <p><i>One more than 6 is 7.<br/>7 is one more than 6.</i></p> <p>Learn to link counting on with adding more than one.</p> $5 + 3 = 8$ |
|                          | <p>Sort people and objects into parts and understand the relationship with the whole.</p>  <p><i>The parts are 4 and 6. The whole is 10.</i></p> | <p>Children draw to represent the parts and understand the relationship with the whole.</p>  <p><i>The parts are 2 and 4. The whole is 6.</i></p> | <p>Use a part-whole model to represent the numbers.</p>  $\boxed{6} + \boxed{4} = \boxed{10}$ $6 + 4 = 10$  |





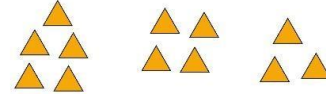

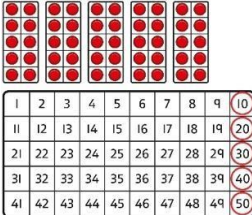
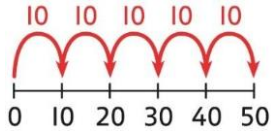

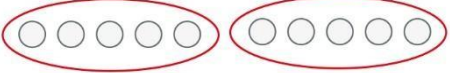
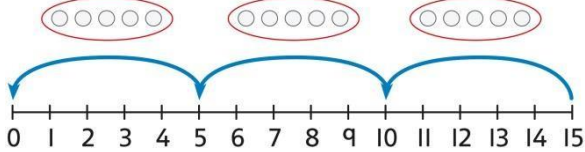
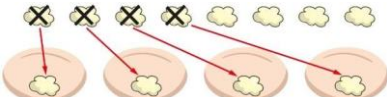

|   |   |  |   |
|---|---|--|---|
| <p><b>Knowing and finding number bonds within 10</b></p>                | <p>Break apart a group and put back together to find and form number bonds.</p>  $3 + 4 = 7$  $6 = 2 + 4$ | <p>Use five and ten frames to represent key number bonds.</p>  $5 = 4 + 1$  $10 = 7 + 3$ | <p>Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.</p> <p>a)</p>  <p>b)</p>  $4 + 0 = 4$ $3 + 1 = 4$ |
| <p><b>Understanding teen numbers as a complete 10 and some more</b></p> | <p>Complete a group of 10 objects and count more.</p>  <p>13 is 10 and 3 more.</p>   | <p>Use a ten frame to support understanding of a complete 10 for teen numbers.</p>  <p>13 is 10 and 3 more.</p>  | <p><b>Understanding teen numbers as a complete 10 and some more.</b></p> <p>1 ten and 3 ones equal 13.</p> $10 + 3 = 13$  |
| <p><b>Adding by counting on</b></p>                                     | <p>Children use knowledge of counting to 20 to find a total by counting on using people or objects.</p>  <p>8 on the bus</p> <p>9 10 11</p>  | <p>Children use counters to support and represent their counting on strategy.</p>  <p>7 on the bus</p>   | <p>Children use number lines or number tracks to support their counting on strategy.</p>  $7 + 5 = \square$  |

|   |  |  |  |
|---|--|--|--|
| <b>Adding the 1s</b>                      | <p>Children use bead strings to recognise how to add the 1s to find the total efficiently.</p>  $2 + 3 = 5$ $12 + 3 = 15$                                       | <p>Children represent calculations using ten frames to add a teen and 1s.</p>  $2 + 3 = 5$ $12 + 3 = 15$                     | <p>Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.</p> $3 + 5 = 8$ <p>So, <math>13 + 5 = 18</math></p> |
| <b>Bridging the 10 using number bonds</b> | <p>Children use a bead string to complete a 10 and understand how this relates to the addition.</p>  <p>7 add 3 makes 10.<br/>So, 7 add 5 is 10 and 2 more.</p> | <p>Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.</p>  | <p>Use a part-whole model and a number line to support the calculation.</p>  $9 + 4 = 13$           |

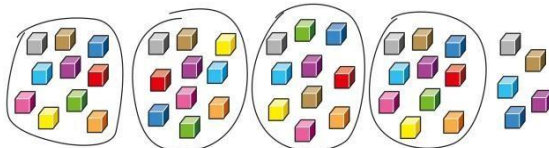
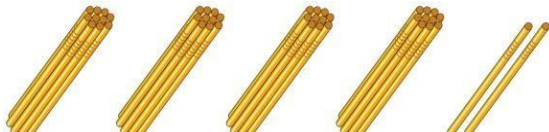
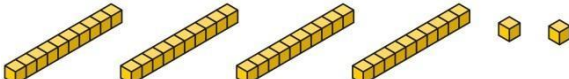
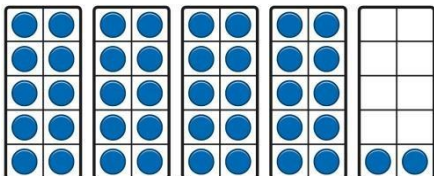
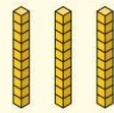

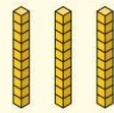

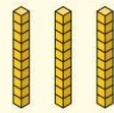


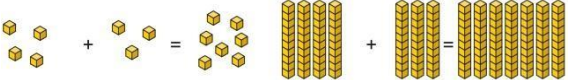
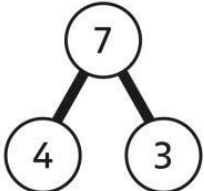
|   |   |  |  |
|---|---|--|--|
| <b>Subtraction Counting back and taking away</b>        | <p>Children arrange objects and remove to find how many are left.</p>  <p>1 less than 10 is 9.<br/>10 subtract 1 is 9.</p>   | <p>Children draw and cross out or use counters to represent objects from a problem.</p>  <p><math>9 - \square = \square</math><br/>There are <math>\square</math> children left.</p> | <p>Children count back to take away and use a number line or number track to support the method.</p>  <p><math>9 - 3 = 6</math></p>   |
| <b>Finding a missing part, given a whole and a part</b> | <p>Children separate a whole into parts and understand how one part can be found by subtraction.</p>  <p><math>8 - 5 = ?</math></p>   | <p>Children represent a whole and a part and understand how to find the missing part by subtraction.</p>  <p><math>5 - 4 = \square</math></p>  | <p>Children use a part-whole model to support the subtraction to find a missing part.</p>  <p><math>7 - 3 = ?</math></p> <p>Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.</p> |
| <b>Finding the difference</b>                           | <p>Arrange two groups so that the difference between the groups can be worked out.</p>  <p>8 is 2 more than 6.<br/>6 is 2 less than 8.</p> <p>The difference between 8 and 6 is 2.</p> | <p>Represent objects using sketches or counters to support finding the difference.</p>  <p><math>5 - 4 = 1</math><br/>The difference between 5 and 4 is 1.</p>                     | <p>Children understand 'find the difference' as subtraction.</p>  <p><math>10 - 4 = 6</math><br/>The difference between 10 and 6 is 4.</p>  |


















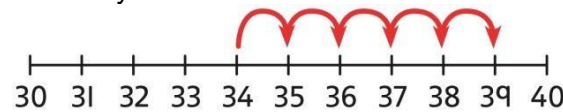




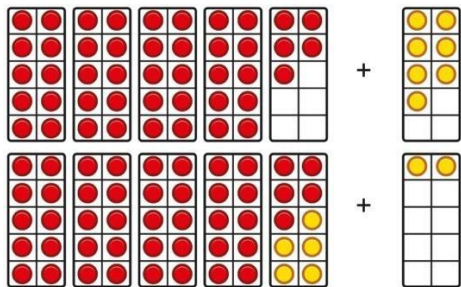
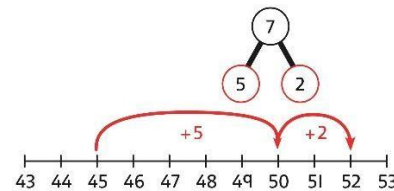
|  |  |   |   |
|--|--|---|---|
| Subtraction within 20                      | <p>Understand when and how to subtract 1s efficiently.</p> <p>Use a bead string to subtract 1s efficiently.</p>  $5 - 3 = 2$ $15 - 3 = 12$  | <p>Understand when and how to subtract 1s efficiently.</p>  $5 - 3 = 2$ $15 - 3 = 12$   | <p>Understand how to use knowledge of bonds within 10 to subtract efficiently.</p> $5 - 3 = 2$ $15 - 3 = 12$  |
| Subtracting 10s and 1s                     | <p>For example: <math>18 - 12</math></p> <p>Subtract 12 by first subtracting the 10, then the remaining 2.</p>  <p><i>First, subtract the 10, then take away 2.</i></p>                                 | <p>For example: <math>18 - 12</math></p> <p>Use ten frames to represent the efficient method of subtracting 12.</p>  <p><i>First, subtract the 10, then subtract 2.</i></p> | <p>Use a part-whole model to support the calculation.</p>  $19 - 14$ $19 - 10 = 9$ $9 - 4 = 5$ <p>So, <math>19 - 14 = 5</math></p> |
| Subtraction bridging 10 using number bonds | <p>For example: <math>12 - 7</math></p> <p>Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.</p>  <p><i>7 is 2 and 5, so I take away the 2 and then the 5.</i></p> | <p>Represent the use of bonds using tenframes.</p>  <p><i>For <math>13 - 5</math>, I take away 3 to make 10, then take away 2 to make 8.</i></p>                           | <p>Use a number line and a part-whole model to support the method.</p> $13 - 5$    |



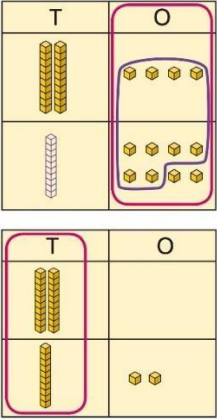
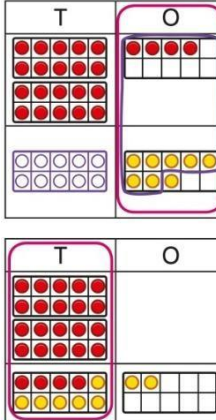


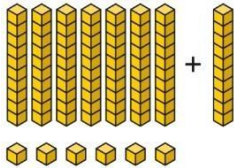

|  |  |   |  |
|--|--|---|--|
| <b>Multiplication</b><br><b>Recognising and making equal groups</b>    | <p>Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.</p> <p>A  B  C </p> | <p>Children draw and represent equal and unequal groups.</p> <p>A  B </p> | <p>Three equal groups of 4.<br/>Four equal groups of 3.</p>  |
| <b>Finding the total of equal groups by counting in 2s, 5s and 10s</b> | <p></p> <p>There are 5 pens in each pack ...<br/>5...10...15...20...25...30...35...40...</p>  | <p>100 squares and ten frames support counting in 2s, 5s and 10s.</p> <p></p>   | <p>Use a number line to support repeated addition through counting in 2s, 5s and 10s.</p> <p></p> |
| <b>Division Grouping</b>   | <p>Learn to make equal groups from a whole and find how many equal groups of a certain size can be made.</p> <p>Sort a whole set people and objects into equal groups.</p> <p> There are 10 children altogether. There are 2 in each group. There are 5 groups</p>                                  | <p>Represent a whole and work out how many equal groups.</p> <p></p> <p>There are 10 in total.<br/>There are 5 in each group. There are 2 groups.</p>      | <p>Children may relate this to counting back in steps of 2, 5 or 10.</p> <p></p>                 |
| <b>Sharing</b>   | <p>Share a set of objects into equal parts and work out how many are in each part.</p> <p></p>  | <p>Sketch or draw to represent sharing into equal parts. This may be related to fractions.</p> <p></p>   | <p>10 shared into 2 equal groups gives 5 in each group.</p>  |

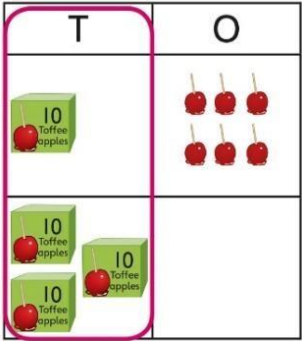
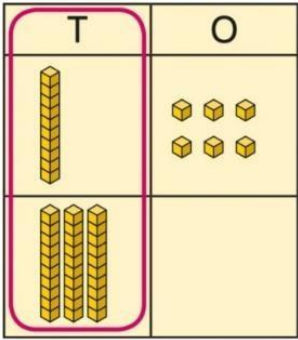
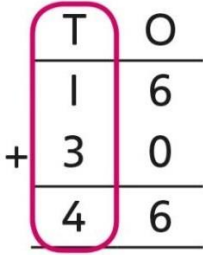
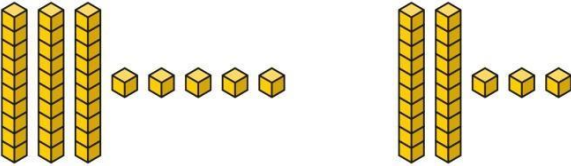
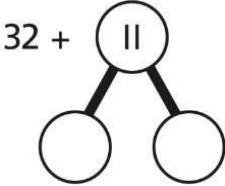
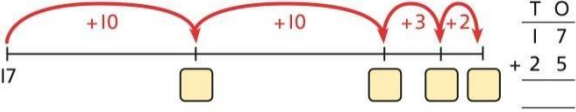
Year 2

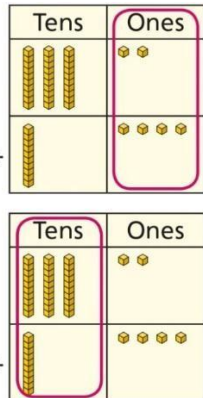
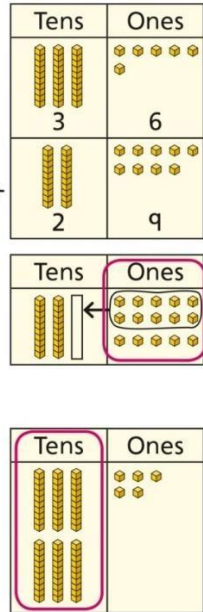
| Year 2  |  |   |  |      |      |   |   |   |   |      |      |   |   |
|---|--|---|--|------|------|---|---|---|---|------|------|---|---|
| Year 2  | Concrete   | Pictorial   | Abstract   |      |      |   |   |   |   |      |      |   |   |
| Understanding 10s and 1s  | <p>Group objects into 10s and 1s.</p>  <p>Bundle straws to understand unitising of 10s.</p>  | <p>Understand 10s and 1s equipment, and link with visual representations on ten frames.</p>   | <p>Represent numbers on a place value grid, using equipment or numerals.</p> <table border="1" data-bbox="1601 426 1910 754"><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td>3</td><td>2</td></tr><tr><th>Tens</th><th>Ones</th></tr><tr><td>4</td><td>3</td></tr></table> | Tens | Ones |  |  | 3 | 2 | Tens | Ones | 4 | 3 |
|   | Tens   | Ones  |  |      |      |   |   |   |   |      |      |   |   |
|  |   |   |  |      |      |   |   |   |   |      |      |   |   |
| 3   | 2  |   |  |      |      |   |   |   |   |      |      |   |   |
| Tens  | Ones   |   |  |      |      |   |   |   |   |      |      |   |   |
| 4   | 3  |   |  |      |      |   |   |   |   |      |      |   |   |
| Adding 10s  | <p>Use known bonds and unitising to add 10s.</p>  <p><i>I know that <math>4 + 3 = 7</math>.<br/>So, I know that 4 tens add 3 tens is 7 tens.</i></p>                         | <p>Use known bonds and unitising to add 10s.</p>  <p><i>I know that <math>4 + 3 = 7</math>.<br/>So, I know that 4 tens add 3 tens is 7 tens.</i></p>                            | <p>Use known bonds and unitising to add 10s.</p>  <p><math>4 + 3 = \square</math></p> <p><math>4 + 3 = 7</math><br/><math>4 \text{ tens} + 3 \text{ tens} = 7 \text{ tens}</math><br/><math>40 + 30 = 70</math></p>  |      |      |   |   |   |   |      |      |   |   |

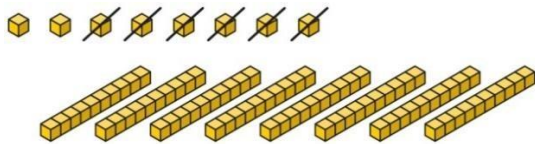
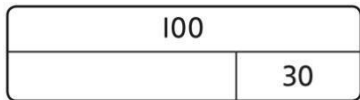
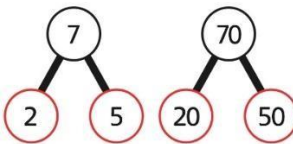
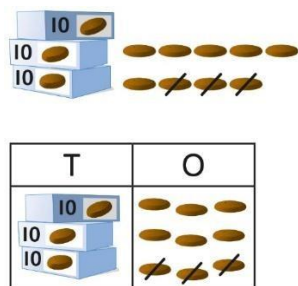
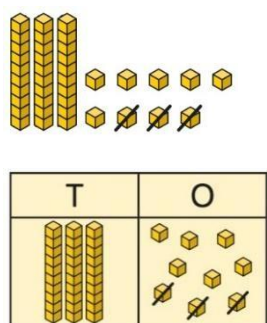
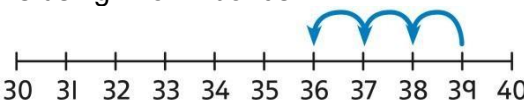
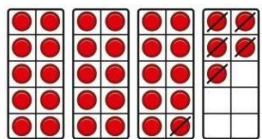
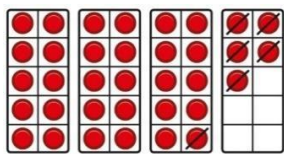
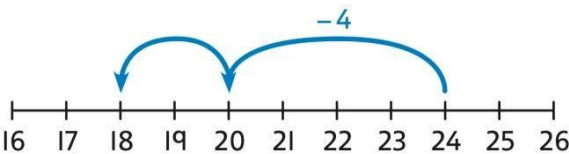
| <p>Adding a 1-digit number to a 2-digit number not bridging a 10</p>  | <p>Add the 1s to find the total. Use known bonds within 10.</p>  <p>41 is 4 tens and 1 one.<br/>41 add 6 ones is 4 tens and 7 ones.</p> <p>This can also be done in a place value grid.</p> <table border="1" data-bbox="235 582 497 853"> <tr> <th>T</th><th>O</th></tr> <tr> <td>  </td><td>  </td></tr> <tr> <td></td><td>  </td></tr> </table> | T | O  |    |  |   |    |   |   |   |   |   |   |  |   |
|---|--|---|--|---|---|---|---|---|---|---|---|---|---|--|---|
| T   | O  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
|    |   |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
|   |   |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| <p>Add the 1s.</p>  <p>34 is 3 tens and 4 ones.<br/>4 ones and 5 ones are 9 ones.<br/>The total is 3 tens and 9 ones.</p> <table border="1" data-bbox="967 518 1247 805"> <tr> <th>T</th><th>O</th></tr> <tr> <td>  </td><td>  </td></tr> <tr> <td></td><td>  </td></tr> </table> | T  | O |  |  |   |  | <p>Add the 1s.</p> <p>Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy.</p>  <p>This can be represented horizontally or vertically.</p> <p><math>34 + 5 = 39</math></p> <p>or</p> <table border="1" data-bbox="1579 758 1736 981"> <tr> <th>T</th><th>O</th></tr> <tr> <td>3</td><td>4</td></tr> <tr> <td>+</td><td>5</td></tr> <tr> <td></td><td>9</td></tr> </table> | T | O | 3 | 4 | + | 5 |  | 9 |
| T   | O  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
|   |   |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
|   |   |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| T   | O  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| 3   | 4  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| +   | 5  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
|   | 9  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| <p>Adding a 1-digit number to a 2-digit number bridging 10</p>  | <p>Complete a 10 using number bonds.</p>  <p>There are 4 tens and 5 ones.<br/>I need to add 7. I will use 5 to complete a 10, then add 2 more.</p>  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |
| <p>Complete a 10 using number bonds.</p>    | <p>Complete a 10 using number bonds.</p>  <p><math>7 = 5 + 2</math><br/><math>45 + 5 + 2 = 52</math></p>  |   |  |   |   |   |   |   |   |   |   |   |   |  |   |




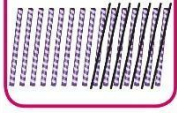



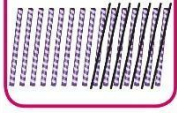





























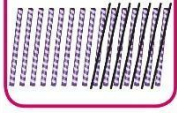













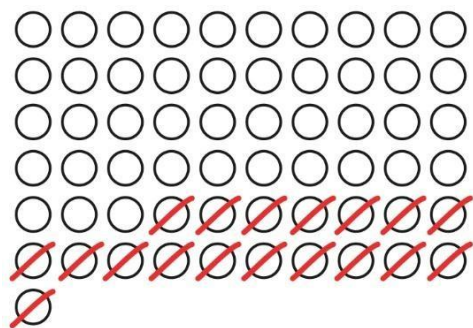
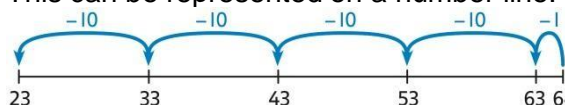
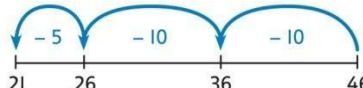


|   |   |   |  |
|---|---|---|--|
| <p>Adding a 1-digit number to a 2-digit number using exchange</p> | <p>Exchange 10 ones for 1 ten.</p>   | <p>Exchange 10 ones for 1 ten.</p>    | <p>Exchange 10 ones for 1 ten.</p>  |
| <p>Adding a multiple of 10 to a 2-digit number</p>                | <p>Add the 10s and then recombine.</p>  <p>27 is 2 tens and 7 ones.<br/>50 is 5 tens.</p> <p>There are 7 tens in total and 7 ones. So, 27 + 50 is 7 tens and 7 ones.</p> | <p>Add the 10s and then recombine.</p>  <p>66 is 6 tens and 6 ones.<br/>66 + 10 = 76</p> <p>A 100 square can support this understanding.</p>  | <p>Add the 10s and then recombine.</p> <p>37 + 20 = ?</p> <p>30 + 20 = 50<br/>50 + 7 = 57</p> <p>37 + 20 = 57</p>      |

|  |  |   |  |
|--|--|---|--|
| <p>Adding a multiple of 10 to a 2-digit number using columns</p> | <p>Add the 10s using a place value grid to support.</p>  <p>16 is 1 ten and 6 ones.<br/>30 is 3 tens.<br/>There are 4 tens and 6 ones in total.</p>   | <p>Add the 10s using a place value grid to support.</p>  <p>16 is 1 ten and 6 ones.<br/>30 is 3 tens.<br/>There are 4 tens and 6 ones in total.</p>   | <p>Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value.</p>  <p> <math>1 + 3 = 4</math><br/> <math>1 \text{ ten} + 3 \text{ tens} = 4 \text{ tens}</math><br/> <math>16 + 30 = 46</math> </p> |
| <p>Adding two 2-digit numbers</p>                                | <p>Add the 10s and 1s separately.</p>  <p> <math>5 + 3 = 8</math><br/>         There are 8 ones in total.<br/><br/> <math>3 + 2 = 5</math><br/>         There are 5 tens in total. <math>35 + 23</math><br/><br/> <math>= 58</math> </p> | <p>Add the 10s and 1s separately. Use an apart-whole model to support.</p>  <p> <math>11 = 10 + 1</math><br/> <math>32 + 10 = 42</math><br/> <math>42 + 1 = 43</math><br/><br/> <math>32 + 11 = 43</math> </p> | <p>Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations.</p>  <p> <math>17 + 25</math> </p>  |


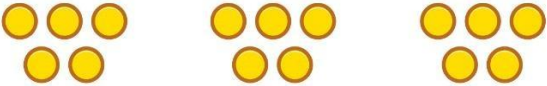
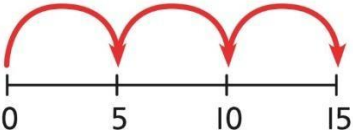

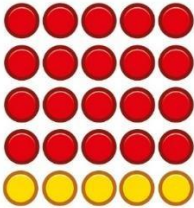
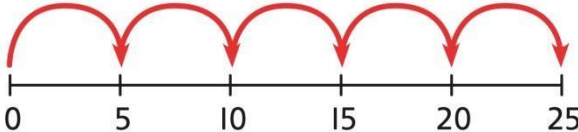



|  |   |  |   |
|--|---|--|---|
| <p>Adding two 2-digit numbers using a place value grid</p> | <p>Add the 1s. Then add the 10s.</p>                               |  | <p>Add the 1s. Then add the 10s.</p> $\begin{array}{r} \text{T} \quad \text{O} \\ 3 \quad 2 \\ + 1 \quad 4 \\ \hline 4 \quad 6 \end{array}$                             |
| <p>Adding two 2-digit numbers with exchange</p>            | <p>Add the 1s. Exchange 10 ones for a ten. Then add the 10s.</p>  |  | <p>Add the 1s. Exchange 10 ones for a ten. Then add the 10s.</p> $\begin{array}{r} \text{T} \quad \text{O} \\ 3 \quad 6 \\ + 2 \quad 9 \\ \hline 6 \quad 5 \end{array}$ |

|  |  |   |  |   |   |   |   |   |   |   |   |
|--|--|---|--|---|---|---|---|---|---|---|---|
| Subtracting multiples of 10                    | <p>Use known number bonds and unitising to subtract multiples of 10.</p>  <p>8 subtract 6 is 2.<br/>So, 8 tens subtract 6 tens is 2 tens.</p> | <p>Use known number bonds and unitising to subtract multiples of 10.</p>  <p><math>10 - 3 = 7</math><br/>So, 10 tens subtract 3 tens is 7 tens.</p> | <p>Use known number bonds and unitising to subtract multiples of 10.</p>  <p>7 tens subtract 5 tens is 2 tens.<br/><math>70 - 50 = 20</math></p>  |   |   |   |   |   |   |   |   |
| Subtracting as single-digit number             | <p>Subtract the 1s. This may be done in or out of a place value grid.</p>    | <p>Subtract the 1s. This may be done in or out of a place value grid.</p>    | <p>Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds.</p>  <table data-bbox="1568 813 1695 973"><tr><td>T</td><td>O</td></tr><tr><td>3</td><td>9</td></tr><tr><td>-</td><td>3</td></tr><tr><td>3</td><td>6</td></tr></table> <p><math>9 - 3 = 6</math><br/><math>39 - 3 = 36</math></p> | T | O | 3 | 9 | - | 3 | 3 | 6 |
| T  | O  |   |  |   |   |   |   |   |   |   |   |
| 3  | 9  |   |  |   |   |   |   |   |   |   |   |
| -  | 3  |   |  |   |   |   |   |   |   |   |   |
| 3  | 6  |   |  |   |   |   |   |   |   |   |   |
| Subtracting as single-digit number bridging 10 | <p>Bridge 10 by using known bonds.</p>  <p><math>35 - 6</math><br/>I took away 5 counters, then 1 more.</p>                                 | <p>Bridge 10 by using known bonds.</p>  <p><math>35 - 6</math><br/>First, I will subtract 5, then 1.</p>  | <p>Bridge 10 by using known bonds.</p>  <p><math>24 - 6 = ?</math><br/><math>24 - 4 - 2 = ?</math></p>  |   |   |   |   |   |   |   |   |

| Subtracting a single-digit number using exchange                                    | <p>Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.</p> <div><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr></table><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr></table></div> | T  | O  |  |  | T  | O  |  |  | <p>Exchange 1 ten for 10 ones.</p> <div><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr></table><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr></table></div> | T | O  |  |  | T  | O  |  |  | <p>Exchange 1 ten for 10 ones.</p> <div><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td>-</td><td></td></tr><tr><td></td><td></td></tr></table><table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td>-</td><td></td></tr><tr><td></td><td></td></tr></table></div> <p><math>25 - 7 = 18</math></p> | T  | O  |  |  | -  |  |    |  | T  | O  |  |  | -  |  |  |  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|---|--|--|----|---|---|----|----|---|---|---|---|----|--|---|----|----|---|---|---|----|----|---|---|----|---|----|---|----|----|---|---|----|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|-----|--|
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|    |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|    |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|   |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|    |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|  |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| -   |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|   |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| T   | O  |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|  |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| -   |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
|  |   |  |    |   |   |    |    |   |   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| Subtracting a 2-digit number  | <p>Subtract by taking away.</p> <div></div> <p><math>61 - 18</math><br/><i>I took away 1 ten and 8 ones.</i></p>   | <p>Subtract the 10s and the 1s.</p> <p>This can be represented on a 100 square.</p> <div><table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr><tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr><tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr><tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr><tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr><tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr><tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr><tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr></table></div> | 1  | 2   | 3   | 4  | 5  | 6   | 7   | 8   | 9 | 10 | 11   | 12  | 13 | 14 | 15  | 16  | 17  | 18 | 19 | 20  | 21  | 22 | 23  | 24 | 25  | 26 | 27 | 28  | 29  | 30 | 31  | 32  | 33  | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | <p>Subtract the 10s and the 1s.</p> <p>This can be represented on a number line.</p> <div></div> <p><math>64 - 41 = ?</math></p> <p><math>64 - 1 = 63</math><br/><math>63 - 40 = 23</math><br/><math>64 - 41 = 23</math></p> <div></div> <p><math>46 - 20 = 26</math><br/><math>26 - 5 = 21</math><br/><math>46 - 25 = 21</math></p> |
| 1   | 2  | 3  | 4  | 5   | 6   | 7  | 8  | 9   | 10  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 11  | 12   | 13   | 14 | 15  | 16  | 17 | 18 | 19  | 20  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 21  | 22   | 23   | 24 | 25  | 26  | 27 | 28 | 29  | 30  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 31  | 32   | 33   | 34 | 35  | 36  | 37 | 38 | 39  | 40  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 41  | 42   | 43   | 44 | 45  | 46  | 47 | 48 | 49  | 50  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 51  | 52   | 53   | 54 | 55  | 56  | 57 | 58 | 59  | 60  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 61  | 62   | 63   | 64 | 65  | 66  | 67 | 68 | 69  | 70  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 71  | 72   | 73   | 74 | 75  | 76  | 77 | 78 | 79  | 80  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 81  | 82   | 83   | 84 | 85  | 86  | 87 | 88 | 89  | 90  |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |
| 91  | 92   | 93   | 94 | 95  | 96  | 97 | 98 | 99  | 100   |   |   |    |  |   |    |    |   |   |   |    |    |   |   |    |   |    |   |    |    |   |   |    |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |     |  |



| Subtracting a 2-digit number using place value and columns | <p>Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid.</p> <table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr></table> <p><math>38 - 16 = 22</math></p>   | T    | O    |  |  | <p>Subtract the 1s. Then subtract the 10s.</p> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr></table> | Tens | Ones |  |      | <p>Using column subtraction, subtract the 1s. Then subtract the 10s.</p> <table><tr><td>T</td><td>O</td></tr><tr><td>4</td><td>5</td></tr><tr><td>- 1</td><td>2</td></tr><tr><td colspan="2"><hr/></td></tr><tr><td></td><td>3</td></tr></table> <table><tr><td>T</td><td>O</td></tr><tr><td>4</td><td>5</td></tr><tr><td>- 1</td><td>2</td></tr><tr><td colspan="2"><hr/></td></tr><tr><td>3</td><td>3</td></tr></table> | T | O | 4    | 5    | - 1 | 2 | <hr/>   |   |   | 3 | T | O   | 4 | 5     | - 1 | 2 | <hr/> |                | 3              | 3   |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|--|---|------|------|--|--|--|------|------|--|------|---|---|---|------|------|-----|---|---|---|---|---|---|-----|---|-------|-----|---|-------|----------------|----------------|-----|---|-------|--|---|---|----------------|----------------|-----|---|-------|--|--|---|---|---|----------------|----------------|-----|---|-------|--|---|---|
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| Tens   | Ones  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| 4  | 5   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 1  | 2   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  | 3   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| 4  | 5   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 1  | 2   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| 3  | 3   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| Subtracting a 2-digit number with exchange                 | <p>Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.</p> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr></table> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr></table> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr></table> <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr></table> | Tens | Ones |  |  | Tens   | Ones |      |  | Tens | Ones  |   |   | Tens | Ones |     |   | <p>Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.</p> <table><tr><td>T</td><td>O</td></tr><tr><td>4</td><td>5</td></tr><tr><td>- 2</td><td>7</td></tr><tr><td colspan="2"><hr/></td></tr></table> <table><tr><td>T</td><td>O</td></tr><tr><td><del>3</del> 4</td><td><sup>1</sup>5</td></tr><tr><td>- 2</td><td>7</td></tr><tr><td colspan="2"><hr/></td></tr></table> <table><tr><td>T</td><td>O</td></tr><tr><td><del>3</del> 4</td><td><sup>1</sup>5</td></tr><tr><td>- 2</td><td>7</td></tr><tr><td colspan="2"><hr/></td></tr><tr><td></td><td>8</td></tr></table> <table><tr><td>T</td><td>O</td></tr><tr><td><del>3</del> 4</td><td><sup>1</sup>5</td></tr><tr><td>- 2</td><td>7</td></tr><tr><td colspan="2"><hr/></td></tr><tr><td>1</td><td>8</td></tr></table> | T | O | 4 | 5 | - 2 | 7 | <hr/> |     | T | O     | <del>3</del> 4 | <sup>1</sup> 5 | - 2 | 7 | <hr/> |  | T | O | <del>3</del> 4 | <sup>1</sup> 5 | - 2 | 7 | <hr/> |  |  | 8 | T | O | <del>3</del> 4 | <sup>1</sup> 5 | - 2 | 7 | <hr/> |  | 1 | 8 |
| Tens   | Ones  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| Tens   | Ones  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| Tens   | Ones  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| Tens   | Ones  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| 4  | 5   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 2  | 7   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <del>3</del> 4   | <sup>1</sup> 5  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 2  | 7   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <del>3</del> 4   | <sup>1</sup> 5  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 2  | 7   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
|  | 8   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| T  | O   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <del>3</del> 4   | <sup>1</sup> 5  |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| - 2  | 7   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| <hr/>  |   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |
| 1  | 8   |      |      |  |  |  |      |      |  |      |   |   |   |      |      |     |   |   |   |   |   |   |     |   |       |     |   |       |                |                |     |   |       |  |   |   |                |                |     |   |       |  |  |   |   |   |                |                |     |   |       |  |   |   |

|   |   |  |  |
|---|---|--|--|
| <p>Equal groups and repeated addition</p>                                 | <p>Recognise equal groups and write as repeated addition and as multiplication.</p>  <p><i>3 groups of 4 chairs<br/>12 chairs altogether</i></p> | <p>Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.</p>  <p><i>3 groups of 5<br/>15 in total</i></p>                                      | <p>Use a number line and write as repeated addition and as multiplication.</p>  <p><math>5 + 5 + 5 = 15</math><br/><math>3 \times 5 = 15</math></p>   |
| <p>Using arrays to represent multiplication and support understanding</p> | <p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><i>4 groups of 5</i></p>                            | <p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><i>4 groups of 5 ... 5 groups of 5</i></p>  | <p>Understand the relationship between arrays, multiplication and repeated addition.</p>  <p><math>5 \times 5 = 25</math></p>   |
| <p>Understanding commutativity</p>  | <p>Use arrays to visualise commutativity.</p>  <p><i>I can see 6 groups of 3. I can see 3 groups of 6.</i></p>                                 | <p>Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.</p>  <p><i>This is 2 groups of 6 and also 6 groups of 2.</i></p> | <p>Use arrays to visualise commutativity.</p>  <p><math>4 + 4 + 4 + 4 + 4 = 20</math><br/><math>5 + 5 + 5 + 5 = 20</math><br/><math>4 \times 5 = 20</math> and <math>5 \times 4 = 20</math></p> |

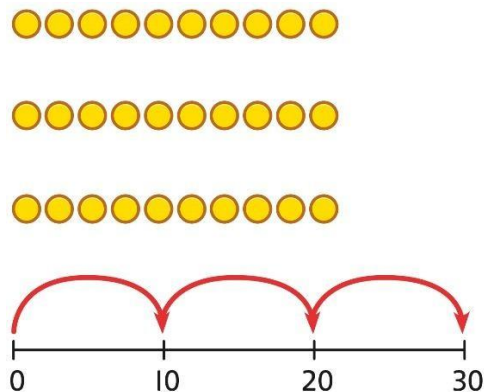
Learning x2,  
x5 and x10 table facts

Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.



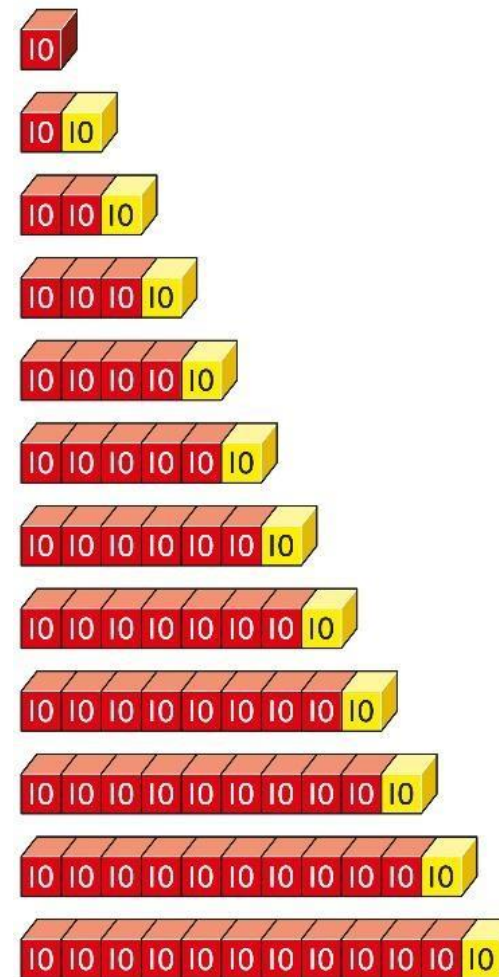
3 groups of 10 ... 10, 20, 30  
 $3 \times 10 = 30$

Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.



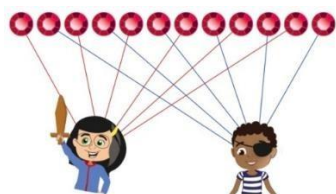
$10 + 10 + 10 = 30$   
 $3 \times 10 = 30$

Understand how the times-tables increase and contain patterns.



$5 \times 10 = 50$   
 $6 \times 10 = 60$

Start with a whole and share into equal parts, one at a time.



*12 shared  
equally  
between  
2. They get  
6 each.*

Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared



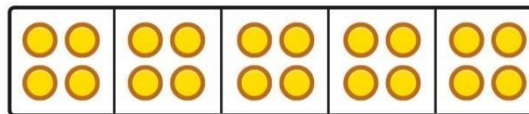
15



They get 5  each.

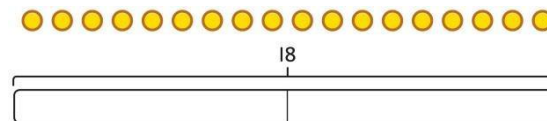
*15 shared equally between 3. They get 5 each.*

Represent the objects shared into equal parts using a bar model.






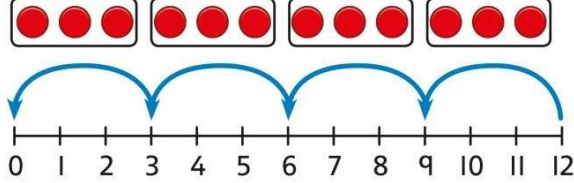
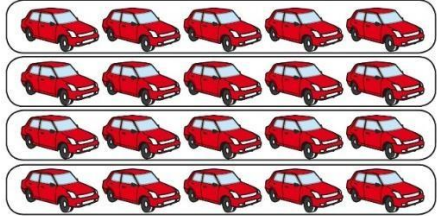
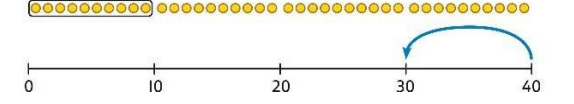
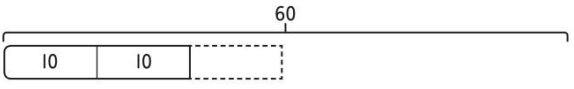


*20 shared into 5 equal parts.  
There are 4 in each part.*

Use a bar model to support understanding of the division.



$$18 \div 2 = 9$$

|  |   |  |   |
|--|---|--|---|
| <p>Grouping equally</p>                            | <p>Understand how to make equal groups from a whole.</p>  <p>8 divided into 4 equal groups. There are 2 in each group.</p>                           | <p>Understand the relationship between grouping and the division statements.</p> <p><math>12 \div 3 = 4</math></p>  <p><math>12 \div 4 = 3</math></p>  <p><math>12 \div 6 = 2</math></p>  <p><math>12 \div 2 = 6</math></p>  | <p>Understand how to relate division by grouping to repeated subtraction.</p>  <p>There are 4 groups now.</p> <p>12 divided into groups of 3.<br/><math>12 \div 3 = 4</math></p> <p>There are 4 groups.</p>  |
| <p>Using known times-tables to solve divisions</p> | <p>Understand the relationship between multiplication facts and division.</p>  <p>4 groups of 5 cars is 20 cars in total. 20 divided by 4 is 5.</p> | <p>Link equal grouping with repeated subtraction and known times-table facts to support division.</p>  <p>40 divided by 4 is 10.</p> <p>Use a bar model to support understanding of the link between times-table knowledge and division.</p>   | <p>Relate times-table knowledge directly to division.</p> <p> <math>1 \times 10 = 10</math><br/> <math>2 \times 10 = 20</math><br/> <math>3 \times 10 = 30</math><br/> <math>4 \times 10 = 40</math><br/> <math>5 \times 10 = 50</math><br/> <math>6 \times 10 = 60</math><br/> <math>7 \times 10 = 70</math><br/> <math>8 \times 10 = 80</math> </p> <p>I used the 10 times-table to help me.<br/><math>3 \times 10 = 30</math>.</p> <p>I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.</p> <p><math>3 \times 10 = 30</math> so <math>30 \div 10 = 3</math></p> |



